

TABLE 1. Lois discrètes classiques

Dénomination	Loi	Espérance	Variance
Loi Uniforme $X \sim \mathcal{U}(\llbracket 1, n \rrbracket)$	$X(\Omega) = \llbracket 1, n \rrbracket$ $\mathbb{P}(X = k) = \frac{1}{n}$	$\mathbb{E}(X) = \frac{n+1}{2}$	$\mathbb{V}(X) = \frac{n^2-1}{12}$
Loi de Bernoulli $X \sim \mathcal{B}(1, p)$	$X(\Omega) = \{0, 1\}$ $\mathbb{P}(X = 0) = 1 - p$ $\mathbb{P}(X = 1) = p$	$\mathbb{E}(X) = p$	$\mathbb{V}(X) = p(1 - p)$
Loi Binomiale $X \sim \mathcal{B}(n, p)$	$X(\Omega) = \llbracket 0, n \rrbracket$ $\mathbb{P}(X = k) = C_n^k p^k (1 - p)^{n-k}$	$\mathbb{E}(X) = np$	$\mathbb{V}(X) = np(1 - p)$
Loi Géométrique $X \sim \mathcal{G}(p)$	$X(\Omega) = \llbracket 1, +\infty \rrbracket$ $\mathbb{P}(X = k) = p(1 - p)^{k-1}$	$\mathbb{E}(X) = \frac{1}{p}$	$\mathbb{V}(X) = \frac{1-p}{p^2}$
Loi de Poisson $X \sim \mathcal{P}(\lambda)$	$X(\Omega) = \llbracket 0, +\infty \rrbracket$ $\mathbb{P}(X = k) = e^{-\lambda} \frac{\lambda^k}{k!}$	$\mathbb{E}(X) = \lambda$	$\mathbb{V}(X) = \lambda$

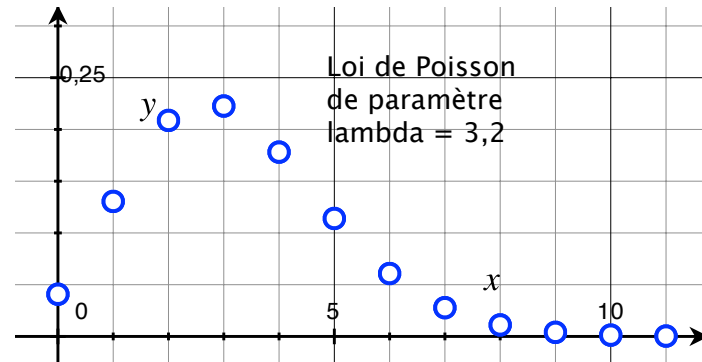
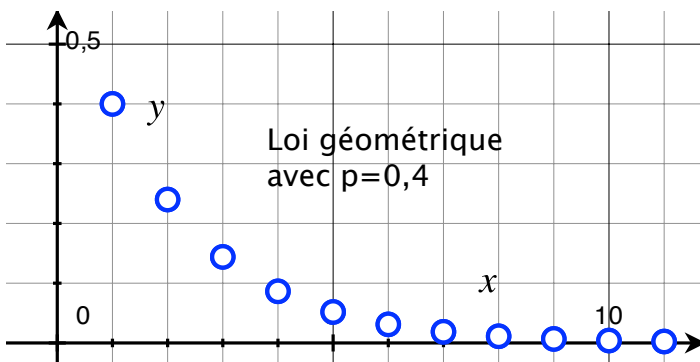
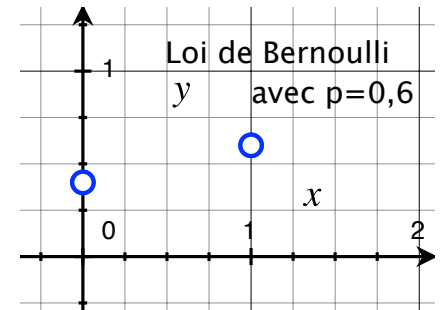
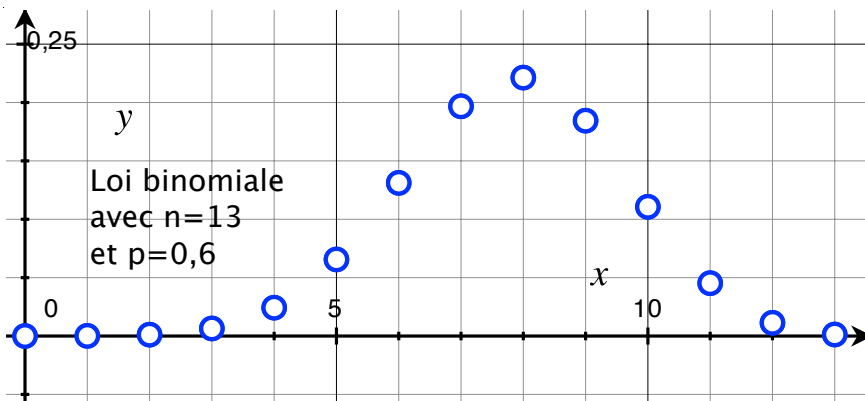
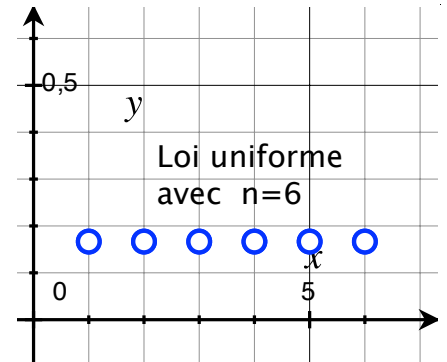
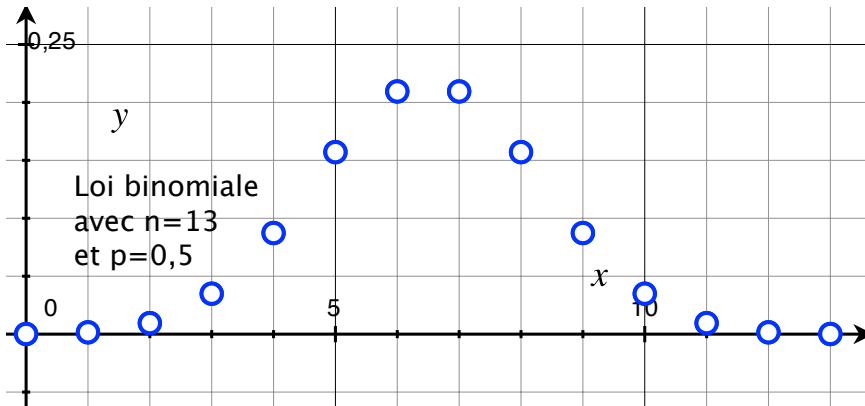
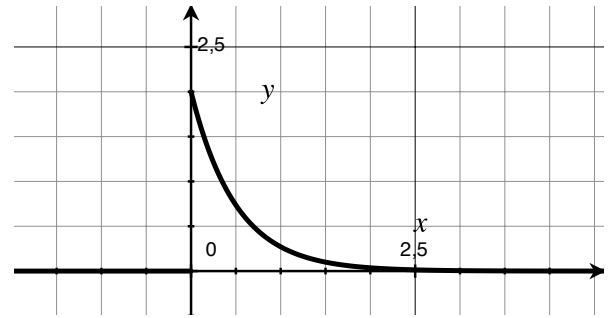
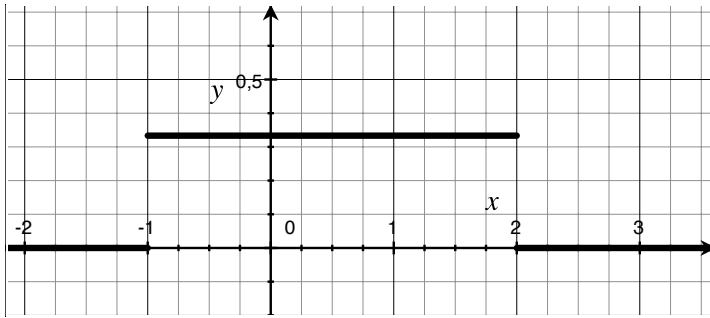
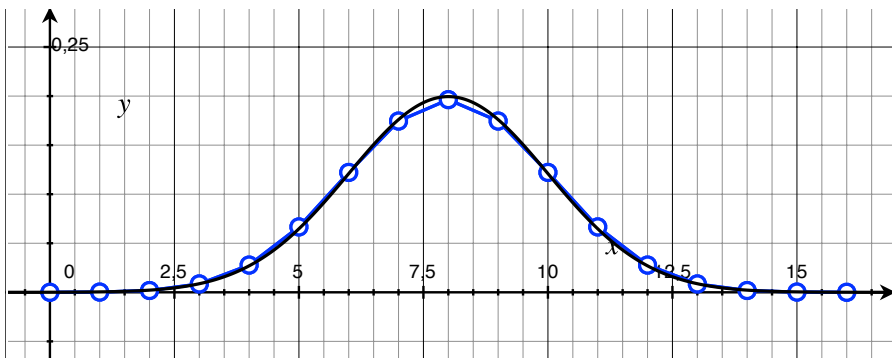
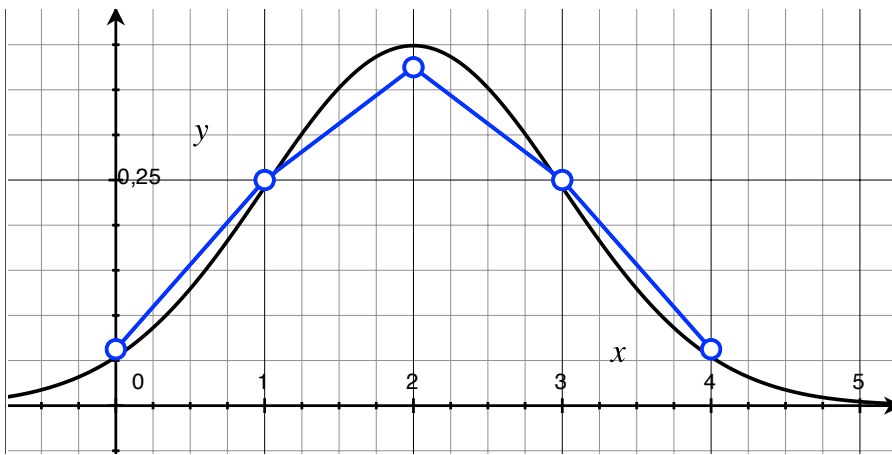


TABLE 2. Lois discrètes classiques

Dénomination	Densité	Espérance	Variance
Loi Uniforme $X \sim \mathcal{U}([a, b])$	$f(x) = \frac{1}{b-a}, \quad x \in [a, b]$ $f(x) = 0, \quad x \notin [a, b]$	$\frac{a+b}{2}$	$\frac{(b-a)^2}{12}$
Loi Exponentielle $X \sim \mathcal{E}(\lambda)$	$f(x) = \lambda e^{-\lambda x}, \quad x \geq 0$ $f(x) = 0, \quad x < 0$	$\frac{1}{\lambda}$	$\frac{1}{\lambda^2}$
Loi Normale $X \sim \mathcal{N}(\mu, \sigma^2)$	$f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}, \quad \forall x \in \mathbb{R}$	$\mu$	$\sigma^2$
Loi Log-Normale Paramètres $\mu, \sigma$	$f(x) = \frac{1}{x\sigma\sqrt{2\pi}} e^{-\frac{(\ln(x)-\mu)^2}{2\sigma^2}}$	$e^{\mu + \frac{\sigma^2}{2}}$	$(e^{\sigma^2} - 1)e^{2\mu + \sigma^2}$
Loi $\chi^2$ (Chi-deux) Paramètre $k \in \mathbb{N}$	$f(x) = \frac{1}{2^{\frac{k}{2}} \Gamma(\frac{k}{2})} x^{\frac{k}{2}-1} e^{-\frac{x}{2}}, \quad x \geq 0$ où $\Gamma$ est la "fonction Gamma" $f(x) = 0, \quad x < 0$	$k$	$2k$
Loi Logistique Paramètres $\mu, s$	$f(x) = \frac{e^{-(x-\mu)/s}}{s(1+e^{-(x-\mu)/s})^2}$	$\mu$	$\frac{\pi^2}{3}s^2$



(a) Loi uniforme  $\mathcal{U}(-1, 2)$ . Sa densité est de  $\frac{1}{3}$  sur l'intervalle  $[-1, 2]$  et de 0 en-dehors de cet intervalle. (b) Densité de la loi exponentielle  $\mathcal{E}(2)$



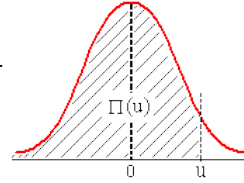
Comparaison de la loi Binomiale  $\mathcal{B}(n, \frac{1}{2})$  avec la loi normale de la même espérance et la même variance, pour  $n = 4$  et  $n = 16$

**Table de Loi Normale**

Fonction de répartition  $\Pi$  de la loi normale centrée réduite.

Probabilité de trouver une valeur inférieure à  $u$ .

$$\Pi(-u) = 1 - \Pi(u)$$



u	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.50000	0.50399	0.50798	0.51197	0.51595	0.51994	0.52392	0.52790	0.53188	0.53586
0.1	0.53983	0.54380	0.54776	0.55172	0.55567	0.55962	0.56356	0.56749	0.57142	0.57535
0.2	0.57926	0.58317	0.58706	0.59095	0.59483	0.59871	0.60257	0.60642	0.61026	0.61409
0.3	0.61791	0.62172	0.62552	0.62930	0.63307	0.63683	0.64058	0.64431	0.64803	0.65173
0.4	0.65542	0.65910	0.66276	0.66640	0.67003	0.67364	0.67724	0.68082	0.68439	0.68793
0.5	0.69146	0.69497	0.69847	0.70194	0.70540	0.70884	0.71226	0.71566	0.71904	0.72240
0.6	0.72575	0.72907	0.73237	0.73565	0.73891	0.74215	0.74537	0.74857	0.75175	0.75490
0.7	0.75804	0.76115	0.76424	0.76730	0.77035	0.77337	0.77637	0.77935	0.78230	0.78524
0.8	0.78814	0.79103	0.79389	0.79673	0.79955	0.80234	0.80511	0.80785	0.81057	0.81327
0.9	0.81594	0.81859	0.82121	0.82381	0.82639	0.82894	0.83147	0.83398	0.83646	0.83891
1.0	0.84134	0.84375	0.84614	0.84849	0.85083	0.85314	0.85543	0.85769	0.85993	0.86214
1.1	0.86433	0.86650	0.86864	0.87076	0.87286	0.87493	0.87698	0.87900	0.88100	0.88298
1.2	0.88493	0.88686	0.88877	0.89065	0.89251	0.89435	0.89617	0.89796	0.89973	0.90147
1.3	0.90320	0.90490	0.90658	0.90824	0.90988	0.91149	0.91309	0.91466	0.91621	0.91774
1.4	0.91924	0.92073	0.92220	0.92364	0.92507	0.92647	0.92785	0.92922	0.93056	0.93189
1.5	0.93319	0.93448	0.93574	0.93699	0.93822	0.93943	0.94062	0.94179	0.94295	0.94408
1.6	0.94520	0.94630	0.94738	0.94845	0.94950	0.95053	0.95154	0.95254	0.95352	0.95449
1.7	0.95543	0.95637	0.95728	0.95818	0.95907	0.95994	0.96080	0.96164	0.96246	0.96327
1.8	0.96407	0.96485	0.96562	0.96638	0.96712	0.96784	0.96856	0.96926	0.96995	0.97062
1.9	0.97128	0.97193	0.97257	0.97320	0.97381	0.97441	0.97500	0.97558	0.97615	0.97670
2.0	0.97725	0.97778	0.97831	0.97882	0.97932	0.97982	0.98030	0.98077	0.98124	0.98169
2.1	0.98214	0.98257	0.98300	0.98341	0.98382	0.98422	0.98461	0.98500	0.98537	0.98574
2.2	0.98610	0.98645	0.98679	0.98713	0.98745	0.98778	0.98809	0.98840	0.98870	0.98899
2.3	0.98928	0.98956	0.98983	0.99010	0.99036	0.99061	0.99086	0.99111	0.99134	0.99158
2.4	0.99180	0.99202	0.99224	0.99245	0.99266	0.99286	0.99305	0.99324	0.99343	0.99361
2.5	0.99379	0.99396	0.99413	0.99430	0.99446	0.99461	0.99477	0.99492	0.99506	0.99520
2.6	0.99534	0.99547	0.99560	0.99573	0.99585	0.99598	0.99609	0.99621	0.99632	0.99643
2.7	0.99653	0.99664	0.99674	0.99683	0.99693	0.99702	0.99711	0.99720	0.99728	0.99736
2.8	0.99744	0.99752	0.99760	0.99767	0.99774	0.99781	0.99788	0.99795	0.99801	0.99807
2.9	0.99813	0.99819	0.99825	0.99831	0.99836	0.99841	0.99846	0.99851	0.99856	0.99861
3.0	0.99865	0.99869	0.99874	0.99878	0.99882	0.99886	0.99889	0.99893	0.99896	0.99900
3.1	0.99903	0.99906	0.99910	0.99913	0.99916	0.99918	0.99921	0.99924	0.99926	0.99929
3.2	0.99931	0.99934	0.99936	0.99938	0.99940	0.99942	0.99944	0.99946	0.99948	0.99950
3.3	0.99952	0.99953	0.99955	0.99957	0.99958	0.99960	0.99961	0.99962	0.99964	0.99965
3.4	0.99966	0.99968	0.99969	0.99970	0.99971	0.99972	0.99973	0.99974	0.99975	0.99976
3.5	0.99977	0.99978	0.99978	0.99979	0.99980	0.99981	0.99981	0.99982	0.99983	0.99983
3.6	0.99984	0.99985	0.99985	0.99986	0.99986	0.99987	0.99987	0.99988	0.99988	0.99989
3.7	0.99989	0.99990	0.99990	0.99990	0.99991	0.99991	0.99992	0.99992	0.99992	0.99992
3.8	0.99993	0.99993	0.99993	0.99994	0.99994	0.99994	0.99994	0.99995	0.99995	0.99995
3.9	0.99995	0.99995	0.99996	0.99996	0.99996	0.99996	0.99996	0.99996	0.99997	0.99997